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Department of Petrochemical Engineering

Subject: Professional Elective (Numerical Method)

Subject Code: BTCHE405

Class: Second Year

Semester: Fourth

Question Bank

1. Solve $x+2y+z=3$; $2x+3y+3z=10$; $3x-y+2z=13$ by gauss elimination method.

2. Solve the following system by Gauss-seidel method:

$$10x-5y-2z=3, 4x-10y+3z= -3, x+6y+10z= -3$$

3. Solve by LU decomposition method of following system:

$$x+y+z=1, 4x+3y-z=6, 3x+5y+3z=4$$

4. $10x-2y-2z=6$; $-x+10y-2z=7$; $-x-y+10z=8$ by Relaxation method.

5. Solve the following system by Gauss-Jacobi method:

$$10x-5y-2z=3, 4x-10y+3z= -3, x+6y+10z= -3$$

6. Solve the following system by Gauss-Elimination method:

$$2x+3y-z=5; \quad 4x+4y-3z=3; \quad 2x-3y+2z=2$$

7. Find the dominant eigen value of $A= \begin{bmatrix} 1 & 2 & 3 & 4 \end{bmatrix}$ by Power method.

8. Find the dominant eigen value of $A= \begin{bmatrix} 25 & 1 & 2 & 1 & 3 & 0 & 2 & 0 & -4 \end{bmatrix}$ by Power method.

9. Determine the coefficient of characteristics polynomial of the system

$$\begin{aligned} (-1 - \lambda)x_1 &= 0 \\ x_1 + (-2 - \lambda)x_2 + 3x_3 &= 0 \\ 2x_2 + (-3 - \lambda)x_3 &= 0 \end{aligned}$$

using Faddeve- Laverrier Method

10. Find the dominant eigen value of $A= \begin{bmatrix} 1 & 6 & 1 & 1 & 2 & 0 & 0 & 0 & 3 \end{bmatrix}$ by Power method.

11. Find the dominant eigen value of $A = \begin{bmatrix} 5 & 0 & 1 \\ 0 & -2 & 0 \\ 1 & 0 & -5 \end{bmatrix}$ by Power method.
12. Find the dominant eigen value of $A = \begin{bmatrix} -4 & -5 \\ 1 & 2 \end{bmatrix}$ by Power method.
13. Solve $x^3 + x^2 - 1 = 0$ by method of Fixed point/Iteration/Successive substations. .
14. Using Newton's method, find the root of $2x^3 - 3x - 6 = 0$ correct to 5 decimal places.
15. Using Newton's Rahson method, find the root between 0 and 1 of $x^3 = 6x - 4$ correct to 5 decimal places.
16. Using Newton's method, find the positive root of $x = \cos x$.
17. Solve $e^x - 3x = 0$ by method of Fixed point/Iteration/Successive substations.
18. Using Newton's method, find the positive root of $3x - \cos x - 1 = 1$.
19. By the method of Least Square method find the best fitting straight line to the data given below:
- | | | | | | |
|----|----|----|----|----|----|
| x: | 5 | 10 | 15 | 20 | 25 |
| y: | 15 | 19 | 23 | 26 | 30 |
20. By the method of Least Square method find the best fitting straight line and y at $x = 2.5$ to the data given below:
- | | | | | | |
|----|-------|-----|-----|-----|---|
| x: | 0 | 1 | 2 | 3 | 4 |
| y: | 1.1.8 | 3.3 | 4.5 | 6.3 | |
21. Find the value of y at $x = 21$ from the following data by Newton's interpolation formula:
- | | | | | |
|----|--------|--------|--------|--------|
| x: | 20 | 23 | 26 | 29 |
| y: | 0.3420 | 0.3907 | 0.4384 | 0.4848 |
22. Using Newton's divided difference formula find the values of $f(2)$ and $f(8)$ from the following table:
- | | | | | | | |
|-------|----|-----|-----|-----|------|------|
| x: | 4 | 5 | 7 | 10 | 11 | 13 |
| f(x): | 48 | 100 | 294 | 900 | 1210 | 2028 |
23. Using Lngrnges interpolation formula, Find $y(10)$ from this data:

x: 5 6 9 11
y: 12 13 14 16

24. By the method of Least Square method find the best fitting straight line of $y = a + bxy$ to the data given below:

x: -4 1 2 3
y: 4 6 10 8

25. Apply Fourth Order Runge Kutta method to find $y(0.2)$ given that $y' = x + y$, $y(0) = 1$.

26. Apply Fourth Order Runge Kutta method to find $y(0.2)$ given that $y' = -y$, $y(0) = 1$.

27. Apply Fourth Order Runge Kutta method to find $y(0.8)$ given that $y' = y - x^2$, $y(0.6) = 1.7379$

28. Compute $y(0.3)$ given $dy/dx + y + xy^2 = 0$, $y(0) = 1$ by RK Method.

29. Given $y' = -y$ and $y(0) = 1$, determine the values of y at $x = (0.01)(0.01)(0.04)$ by Euler method.

30. $x^3 - 2x^2 - 3x - 4 = 0$ whose root lies between 3 and 4. Find the real root of equation by using Newton Raphson Method. Correct upto 4 decimal places.

31. Solve the following set of linear algebraic equations by using Gauss Elimination method correct upto 4 decimal places.

$$6x - y + z = 13$$

$$x + y + z = 9$$

$$10x + y - z = 19$$

32. Solve the following set of nonlinear algebraic equations by using Multivariable Newton Raphson method correct upto 4 decimal points.

$xy = x^2 + 3$ and $y^2 = 2xy - 8$ using $(x_0, y_0) = (3.1, 3.9)$ for two iterations.

33. Using the Newton's divided difference interpolation find $y(10)$ given that

$$y(5)=12, y(6)=13, y(9)=14, y(11)=16$$

34. Use Runge Kutta method of 4'th order to solve $\frac{dy}{dx} = \frac{y^2-x^2}{y^2+x^2}$ with $y(0)=1$ at $x=0.2$ $x=0.4$

Solve to 4 decimal places.

35. Using Second Order Runge Kutta method find $y(0.1), y(0.2)$ given $\frac{dy}{dx} = x^2 + y^2$ $y(0)=1$.

36. Find the real root of $x^3 = 1 - x^2$ equation by using Fixed point method.

Correct upto 2 decimal places.

37. Find the real root of $3x - \cos x - 1 = 0$ by Newton Raphson Method.

Correct upto 4 decimal places.

38. Solve the following boundary value problems $(1+x^2)y'' + 4xy' + 2y = 2$ $y(0)=0, y(1)=\frac{1}{2}$ by the Finite difference method. Use central difference approximation with $h=1/3$.

39. Use Runge Kutta method of 4'th order to solve $\frac{dy}{dx} = \frac{y^2-x^2}{y^2+x^2}$ with $y(0)=1$ at $x=0.2$ $x=0.4$

Solve to 4 decimal places.

40. Using Second Order Runge Kutta method find $y(0.1), y(0.2)$ given $\frac{dy}{dx} = x^2 + y^2$ $y(0)=1$.

41. Solve the following set of nonlinear algebraic equations by using Multivariable Newton Raphson method correct upto 4 decimal points.

$$xy = x^2 + 3 \quad \text{and} \quad y^2 = 2xy - 8 \quad \text{using} \quad (x_0, y_0) = (3.1, 3.9) \quad \text{for two iterations.}$$

42. Solve the system of linear algebraic equations by using Crout's method.

$$4x + 2y + z = 3$$

$$4x + 3y + 2z = 4$$

$$x + 5y - 2z = 6$$