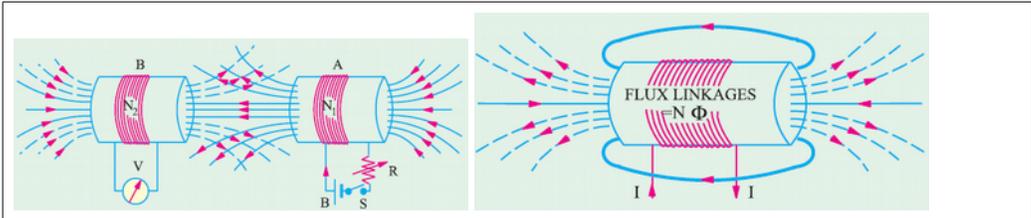
	
3.a)	<p>i) RMS value: RMS value is the effective value of a varying voltage or current. It is the equivalent steady (DC) value which will produce same heat in the same resistor in the same time. $V_{rms} = V_m / \sqrt{2}$</p> <p>ii) Form factor: FF for particular waveform is defined as the ration of the rms value to the average value. $FF = \text{Rms value} / \text{Avg Value} = 1.11$ for sinusoidal waveform</p> <p>iii) Peak factor: It is defined as the ratio of the peak of value to the rms value $K_p = \text{peak value} / \text{Rms value} = 1.414$ sinusoidal waveform</p>	2 2 2
b)	<p>$V_1 = 100 \sin 314t$ $V_2 = 150 \sin (314t + \pi/6)$ given voltage phasors resolve each voltage phasors vertically and horizontally and find combined V_x and V_y components $V_x = 100 \cos 0 + 150 \cos(\pi/6) = 229.9 \text{ V}$ $V_y = 100 \sin(0) + 150 \sin(\pi/6) = 75 \text{ V}$ $V_{xy} = \text{resultant phasor} = \sqrt{(V_x)^2 + (V_y)^2} = 241 \text{ V}$ The angle between resultant phasor and ref V_1 $\tan(\alpha) = V_x / V_y$ $\alpha = 18^\circ$ $V_{xy} = 241 \sin(314t + 18)$</p> <p>Phasor diagram</p>	2 3 1
or b)	<p>current through $100 \mu\text{F}$ cap $i_c = (V_m / X_c) * (\sin 2\pi f t + \pi/2)$ $X_c = 1 / (2\pi f C) = 1.59 \text{ ohm}$ $i_c = 9.42 \sin(2000\pi t + \pi/2)$ Phasor diagram: Voltage and cap current</p>	3 3
4.a)	<p>series resonance: A resonance in series RLC circuit is condition when the supply voltage and current are in phase and the circuit impedance at resonance is purely resistive. Consider a general series circuit with R, L and C connected across sinusoidal voltage source of constant voltage magnitude and variable frequency. Total circuit impedance $Z = \sqrt{R^2 + (X_L - X_C)^2}$ at resonance $X_L = X_C$ i.e. $Z_0 = R$ Current at resonance $= I_0 = V / Z_0 = V / R$ V and I_0 are in phase $PF = \cos \Phi_0 = 1$ Power absorbed by circuit $P_0 = V^2 / R$ Resonant frequency $= f_0 = 1 / (2\pi \sqrt{LC})$</p>	4

	circuit diagram	2
b)	$Z_1=R_1+jX_{L1}$ $Z_2=R_2+jX_{L2}$ total circuit impedance (Z)= $Z_1+Z_2=16+j10.99$ since series connection Total current (I)= $V/Z=11.85 \angle -34.48^\circ$ A phasor diagram:	2 2 2
5. a)	Statically Induced E.M.F.divided into (a) mutually induced e.m.f. and (b) self-induced e.m.f. (a) Mutually-induced e.m.f. Consider two coils A and B lying close to each other (Fig.).Coil A is joined to a battery, a switch and a variable resistance R where as coil B is connected to a sensitive voltmeter V . When current through A is established by closing the switch, its magnetic field is set up which partly links with or threads through the coil B . As current through A is changed, the flux linked with B is also changed. Hence, mutually induced e.m.f. is produced in B whose magnitude is given by Faraday's Laws and direction by Lenz's Law. If, now, battery is connected to B and the voltmeter across A , then the situation is reversed and now a change of current in B will produce mutually-induced e.m.f. in A . It is obvious that in the examples considered above, there is no movement of any conductor, the flux variations being brought about by variations in current strength only. Such an e.m.f. induced in one coil by the influence of the other coil is called (statically but) mutually induced e.m.f.	3
		3
	(b) Self-induced e.m.f. This is the e.m.f. induced in a coil due to <i>the change of its own flux linked with it</i> . If current through the coil Fig. is changed, then the flux linked with its own turns will also change, which will produce in it what is called <i>self-induced</i> e.m.f. The direction of this induced e.m.f. (as given by Lenz's law) would be such as to oppose any change of flux which is, in fact, the very cause of its production. Hence, it is also known as the <i>opposing or counter e.m.f. of self-induction</i> .	
b.	$l=15\text{ cm}=0.15\text{m}$ $a=1\text{cm}^2=1\times 10^{-4}\text{m}^2$ permeability of Iron= 2400 turns= 1800 $\Phi=0.2\text{mWb}=0.2\times 10^{-3}\text{Wb}$ Reluctance(S)= $l/(\mu_0\mu_r a)=4.97\times 10^5\text{A/wb}$ $I=(S\Phi)/N=55.22\text{mA}$	3 3
6 a)	EMF equation of transformer: Let the flux at any instant be given by $\phi = \phi_m \sin \omega t$ (1) According to faradays law instantaneous emf induced in a coil of T turns $e = -(d(\phi T)/dt) = -T\omega\phi_m \cos\omega t$ $e = T\omega\phi_m \sin(\omega t - \pi/2) = E_m \sin(\omega t - \pi/2)$ where $E_m = T\omega\phi_m$ is the maximum value of e for a sine wave the rms value is given by $E = E_m/\sqrt{2} = 2\pi f T \phi_m/\sqrt{2}$ $E = 4.44 \phi_m f T$	6

b)

Charging of capacitor: Capacitor C may be charged through a high resistance R from a battery of V volts. For charging, the battery is connected across the RC series circuit. The voltage across C does not rise to V instantaneously but builds up slowly i.e. exponentially and not linearly. Charging current i_c is maximum at the start i.e. when C is uncharged, then it decreases exponentially and finally ceases when p.d. across capacitor plates becomes equal and opposite to the battery voltage V . At any instant during charging, let $v_c =$ p.d. across C ; $i_c =$ charging current $q =$ charge on capacitor plates

6

The applied voltage V is always equal to the sum of :

(i) resistive drop ($i_c R$) and (ii) voltage across capacitor (v_c)

$$\therefore V = i_c R + v_c$$

$$\text{Now } i_c = \frac{dq}{dt} = \frac{d}{dt}(Cv_c) = C \frac{dv_c}{dt} \therefore V = v_c + CR \frac{dv_c}{dt}$$

$$\text{or } -\frac{dv_c}{V - v_c} = -\frac{dt}{CR}$$

$$\text{Integrating both sides, we get } \int \frac{-dv_c}{V - v_c} = -\frac{1}{CR} \int dt; \therefore \log_e (V - v_c) = -\frac{t}{CR} + K$$

where K is the constant of integration whose value can be found from initial known conditions. We know that at the start of charging when $t = 0$, $v_c = 0$.

Substituting these values in (iii), we get $\log_e V = K$

$$\text{Hence, Eq. (iii) becomes } \log_e (V - v_c) = \frac{-t}{CR} + \log_e V$$

$$\text{or } \log_e \frac{V - v_c}{V} = \frac{-t}{CR} = -\frac{t}{\lambda} \text{ where } \lambda = CR = \text{time constant}$$

$$\therefore \frac{V - v_c}{V} = e^{-t/\lambda} \text{ or } v_c = V (1 - e^{-t/\lambda})$$

This gives variation with time of voltage across the capacitor plates and is shown in Fig.

Time Constant: Time constant may be defined as the time during which capacitor voltage actually rises to 0.632 of its final steady value.